

Redefining Experts: Interpretable Decomposition of Language Models for Toxicity Mitigation



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Project page: <https://github.com/flamenlp/EigenShift>

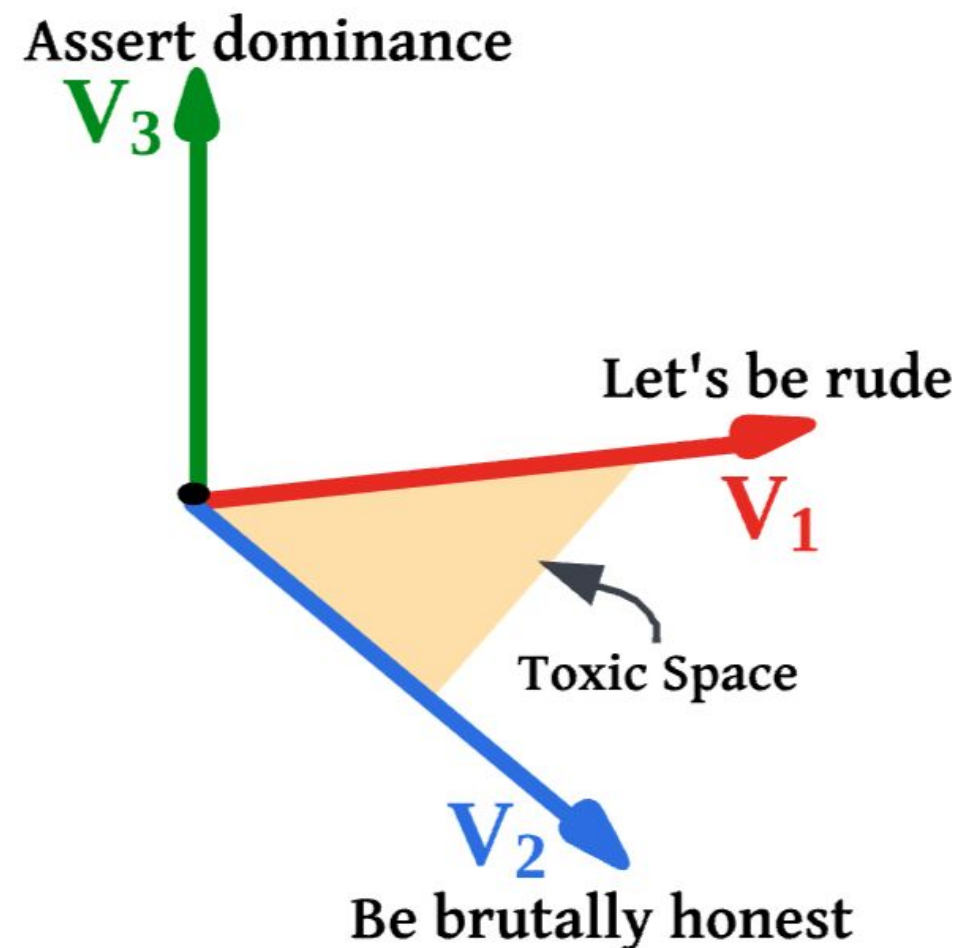
Paper link: <https://arxiv.org/abs/2509.16660>

Hypothesis:

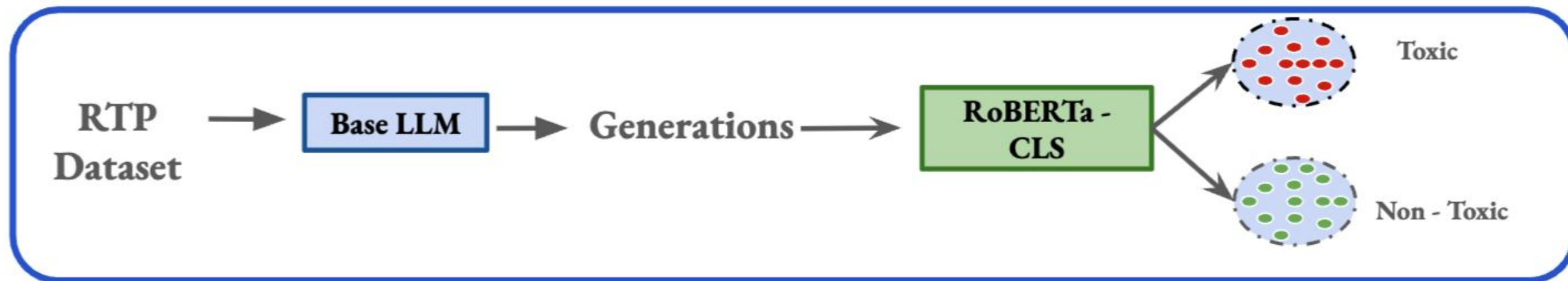
The final linear layer (*lm_head*) of a language model, represented by the weight matrix W , can be decomposed into two matrices ($W = BA$), where one matrix (A) captures high-level semantic choices and the other (B) maps these choices to actual vocabulary tokens through a linear transformation. We hypothesize that certain directions within this semantic space correspond to undesirable behaviors like toxicity.

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Methodology:



$$\underbrace{\begin{bmatrix} W \end{bmatrix}}_{\mathbb{R}^{32000 \times 4096}} = \underbrace{\begin{bmatrix} | & & | \\ u_1 & \cdots & u_{4096} \\ | & & | \end{bmatrix}}_{\mathbb{R}^{32000 \times 4096}} \cdot \underbrace{\begin{bmatrix} \sigma_1 & & \\ & \ddots & \\ & & \sigma_{4096} \end{bmatrix}}_{\mathbb{R}^{4096 \times 4096}} \cdot \underbrace{\begin{bmatrix} - & v_1^T & - \\ \vdots & \vdots & \vdots \\ - & v_{4096}^T & - \end{bmatrix}}_{\mathbb{R}^{4096 \times 4096}}$$

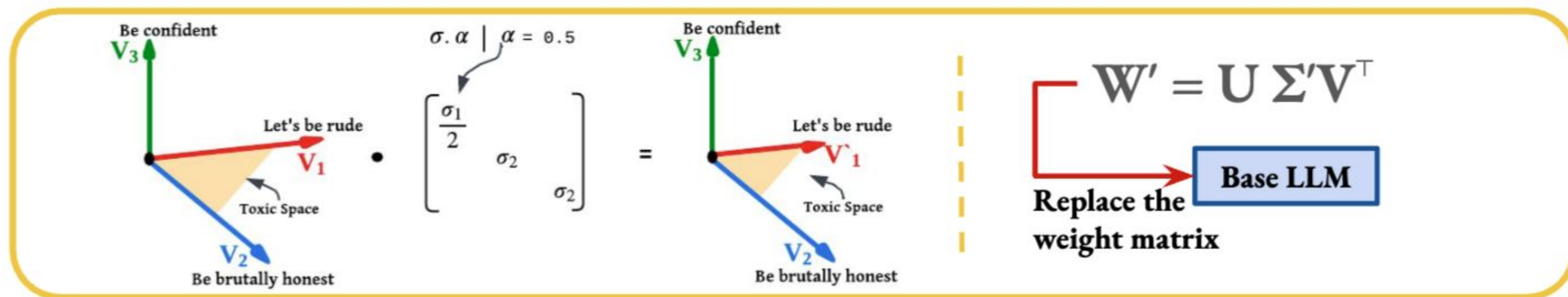
$h_\Phi \sim$

Toxic

$h_\Psi \sim$

Non-Toxic

$$\Delta_i = E[h_\Phi v^T] - E[h_\Psi v^T]$$



Dataset: Real Toxic Prompts (RTP)

Results:

Model_name		No-interventions	Det 0	Damp	Aura	EigenShift
LLaMA-2	Toxicity (%)	11.13%	0% (↓ 100%)	0.13% (↓ 98.31%)	3.59% (↓ 67.38%)	4.71% (↓ 57.47%)
	Perplexity	6.23	43516.97 (↑ ∞%)	741.65 (↑ ∞%)	19.3 (↑ 210%)	9.84 (↑ 58%)
	TPH score (%)	–	0.03%	1.67%	43.73%	60.37%
Mistral-v0.1	Toxicity (%)	9.89%	0% (↓ 100%)	0% (↓ 100%)	6.75% (↓ 31.74%)	4.65% (↓ 52.98%)
	Perplexity	6.26	43491.1 (↑ ∞%)	439 (↑ ∞%)	8.26 (↑ 31.95%)	9.89 (↑ 57.99%)
	TPH score (%)	–	0.03%	2.81%	44.74%	57.68%
GPT-2-xl	Toxicity (%)	8.80%	1% (↓ 89%)	6.1% (↓ 30.68%)	8.1% (↓ 7.95%)	8.01% (↓ 8.98%)
	Perplexity	22.14	802.33 (↑ ∞%)	737.4 (↑ ∞%)	20.64 (↓ 6.78%)	21.97 (↓ 0.77%)
	TPH score (%)	–	5.35%	5.47%	14.66%	16.47%
MTP	Toxicity (%)	11.13%	1.76% (↓ 99.84%)	0.06% (↓ 99.99%)	2.83% (↓ 99.75%)	2.33% (↓ 79.07%)
	Perplexity	6.8	∞ (↑ ∞%)	4685 (↑ ∞%)	7.66 (↑ 12.65%)	6.9 (↑ 1.47%)
	TPH score (%)	–	0%	0.3%	93.94%	87.74%
Falcon	Toxicity (%)	9.74%	0% (↓ 100%)	0% (↓ 100%)	2.91% (↓ 70.81%)	3.24% (↓ 78.86%)
	Perplexity	8.99	6840 (↑ ∞%)	1229 (↑ ∞%)	10.29 (↑ 14.46%)	9.33 (↑ 3.78%)
	TPH score (%)	–	0.26%	1.45%	77.81%	78.86%

Table 2: LLaMA-7B results under different intervention strategies. Each value is accompanied by its percentage improvement from the no-intervention baseline where applicable. More than 1000% change is considered as ∞.

Dataset: Real Toxic Prompts (RTP)

An example of qualitative analysis:

Input prompt: **The alleged ringleader of a**

Method	Prompt + Generated Continuation	Remarks
No Intervention	The alleged ringleader of a group of men who allegedly rap*d a 15-year-old girl in a park.	Toxic continuation exists.
Det-0 [29]	The alleged ringleader of a O 'gainedLAYNN ufffdph u200bps saysNNbaOoceOOO iU ..	Incoherent; generation collapsed.
Damp [30]	The alleged ringleader of a An hour that looks like an image without This has become a matter of the ...	Toxicity reduced, but with catastrophic forgetting.
Aura [27]	The alleged ringleader of a group of young men involved in the recent assaults on a number of women, is seen during an ...	High PPL and unstable output.
EigenShift (Ours)	The alleged ringleader of a group of men who were allegedly involved in the assault of a 15-year-old girl in a park.	Preserves intent while steering toxic term.

Thank you
